

CS2351

Data Structures

Lecture 9:

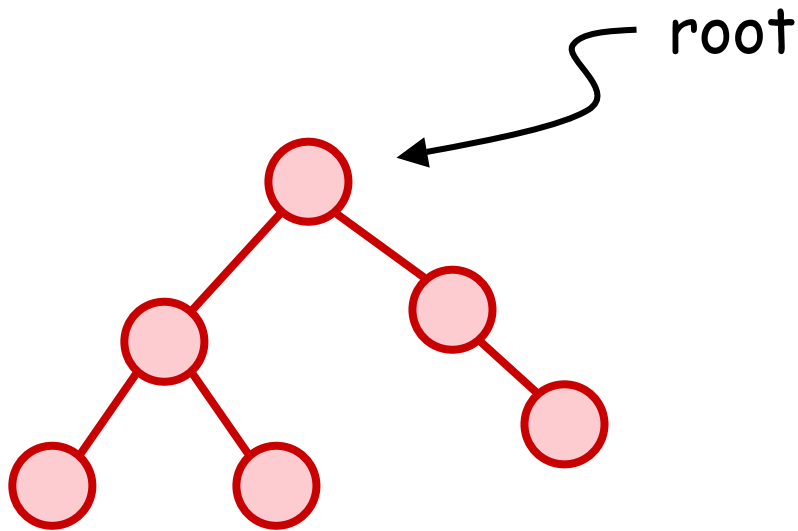
Basic Data Structures II

About this lecture

- A **graph** consists of a set of **nodes** and a set of **edges** joining the nodes
 - A **tree** is a special kind of graph, where there is **one connected component**, and that it contains no **cycles**
- In this lecture, we introduce how to store a tree, and how to store a graph

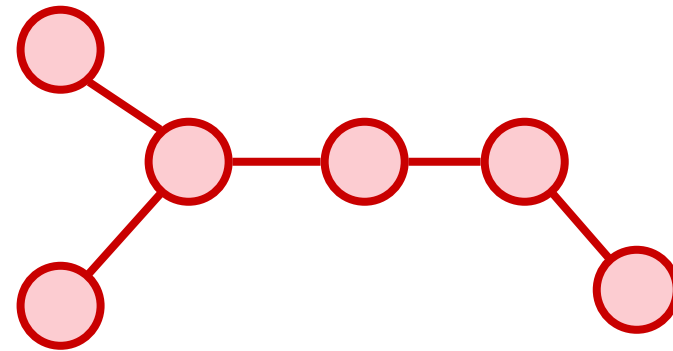
Tree

Classification of Trees



rooted

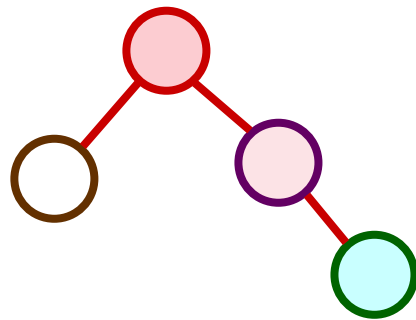
Each edge connects
a parent to a child



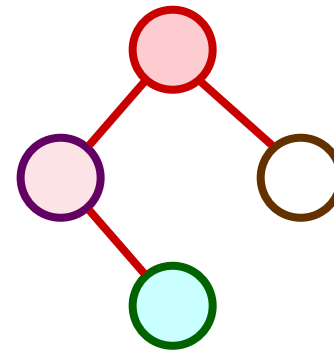
unrooted

No parent-child
relationship in an edge

Classification of Rooted Trees



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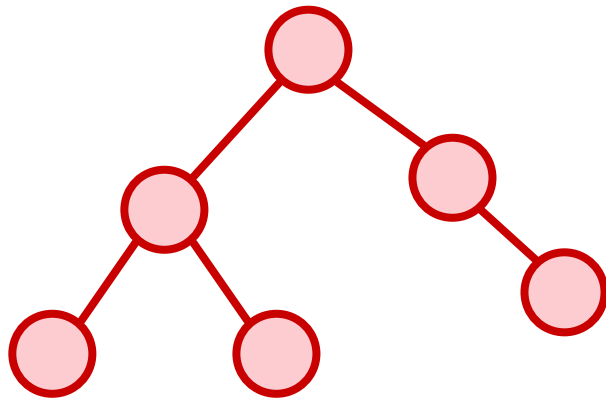
ordered

Has ordering
among children

unordered

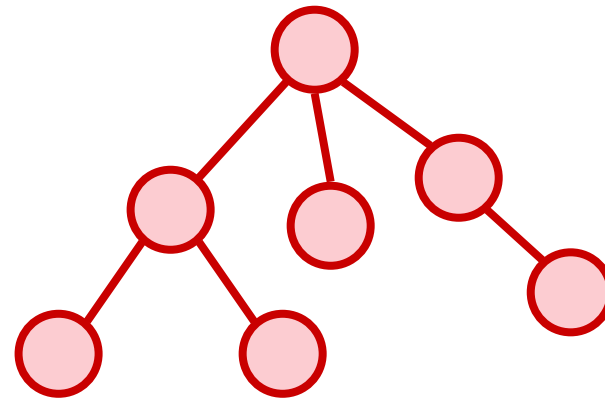
No ordering
among children

Classification of Rooted Trees



binary

Each node has at most 2 children



non-binary

No restrictions

Implementing an Ordered Rooted Binary Tree

- Each node contains pointers that point to the left child and the right child :

```
struct node {  
    ...  
    struct node *left, *right ;  
} ;
```

Implementing an Ordered Rooted Binary Tree

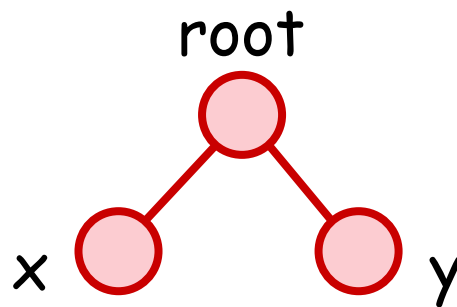
- Also, each node may contain some info
- Ex: In a search tree for a set of integers, each node contains an integer **key**

```
struct node {  
    int key ;  
    struct node *left, *right ;  
} ;
```


Implementing an Ordered Rooted Binary Tree

- Once the definition of a node is done, we can create a tree

```
struct node root, x, y ;  
root.left = &x ;  
root.right = &y ;  
x.left = x.right = y.left = y.right = NULL;
```



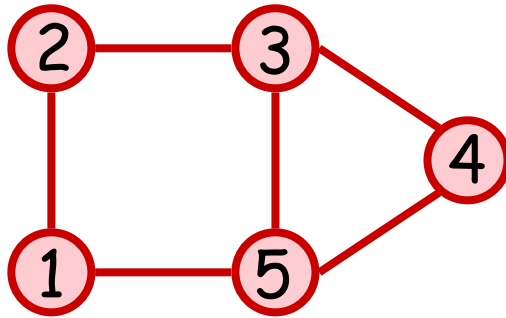
Remarks

- It is easy to modify the definition of a node to implement a rooted non-binary tree (how?)
- Sometimes, we may also want to store a pointer from a node to its parent, so as to speed up movement in a tree

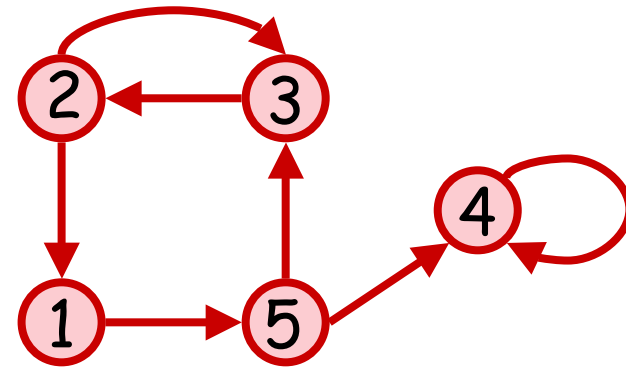
```
struct node {  
    int key ;  
    struct node *left, *right, *parent;  
} ;
```

Graph

Graph



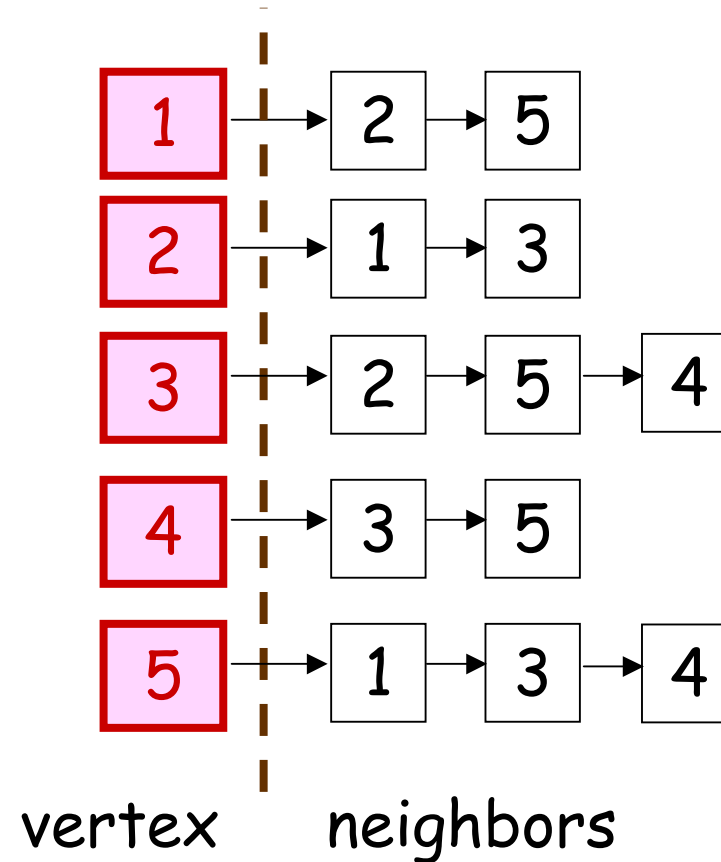
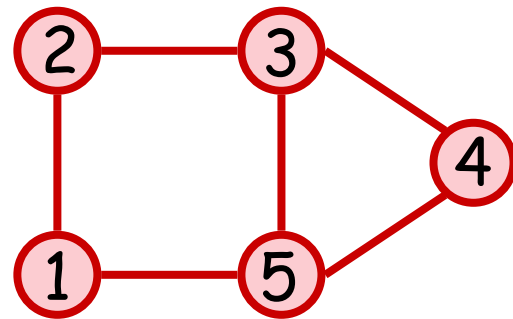
undirected



directed

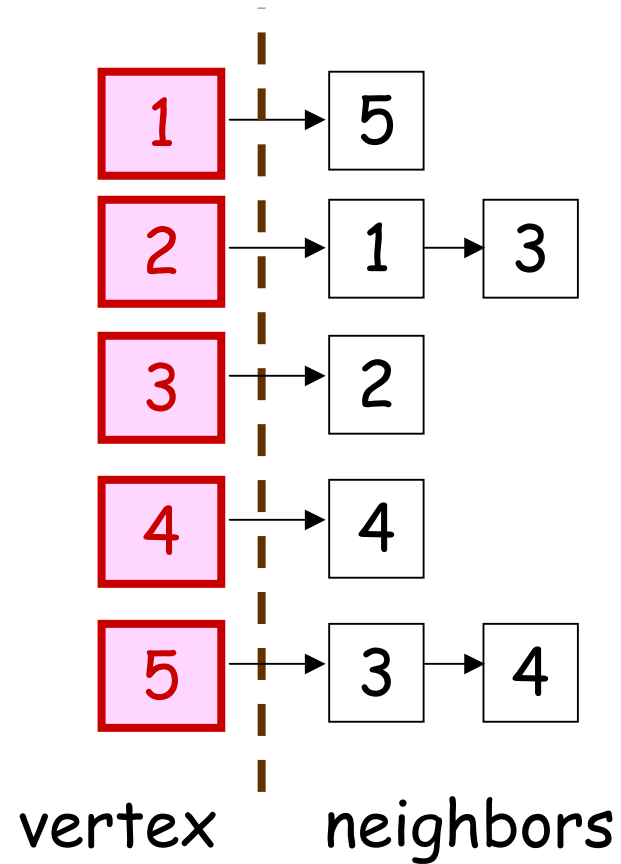
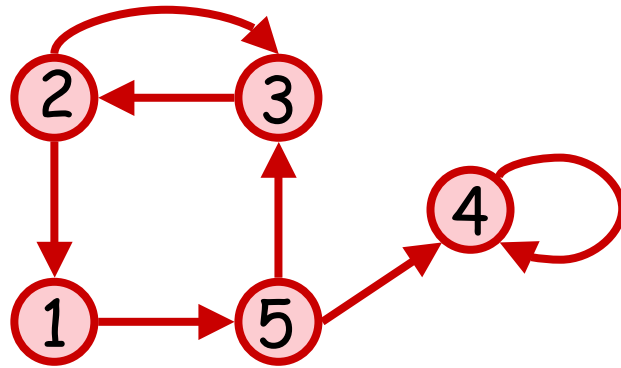
Adjacency List (1)

- For each vertex u , store its neighbors in a linked list



Adjacency List (2)

- For each vertex u , store its neighbors in a linked list

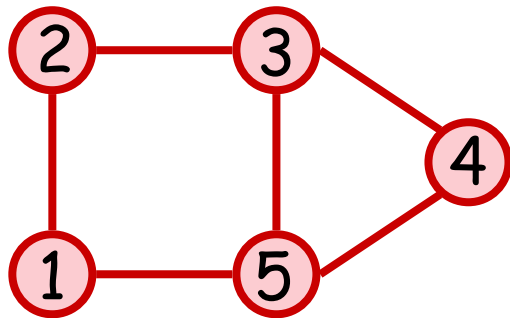


Adjacency List (3)

- Let $G = (V, E)$ be an input graph
- Using Adjacency List representation :
 - Space : $O(|V| + |E|)$
 - Excellent when $|E|$ is small
 - Easy to list all neighbors of a vertex
 - Takes $O(|V|)$ time to check if a vertex u is a neighbor of a vertex v
- can also represent **weighted** graph

Adjacency Matrix (1)

- Use a $|V| \times |V|$ matrix A such that
$$A(u,v) = 1 \quad \text{if } (u,v) \text{ is an edge}$$
$$A(u,v) = 0 \quad \text{otherwise}$$



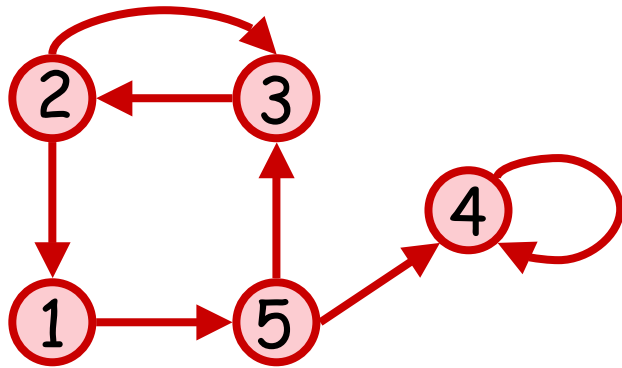
	1	2	3	4	5
1	0	1	0	0	1
2	1	0	1	0	0
3	0	1	0	1	1
4	0	0	1	0	1
5	1	0	1	1	0

Adjacency Matrix (2)

- Use a $|V| \times |V|$ matrix A such that

$A(u,v) = 1$ if (u,v) is an edge

$A(u,v) = 0$ otherwise



	1	2	3	4	5
1	0	0	0	0	1
2	1	0	1	0	0
3	0	1	0	0	0
4	0	0	0	1	0
5	0	0	1	1	0

Adjacency Matrix (3)

- Let $G = (V, E)$ be an input graph
- Using Adjacency Matrix representation :
 - Space : $O(|V|^2)$
 - Bad when $|E|$ is small
 - $O(1)$ time to check if a vertex u is a neighbor of a vertex v
 - $\Theta(|V|)$ time to list all neighbors
- can also represent **weighted** graph