# CS5321 Numerical Optimization Homework 1 

Due March 10

1. $(30 \%)$ For a single variable function $f(x)$, its derivative represents the slop of its tangent. But the concept of slope is only for two dimensional lines. Actually, the geometrical meaning of $f^{\prime}(x)$ is also associated with the normal vector if we treat the $(x, f(x))$ as a curve on a two-dimensional space. The normal vector, or simply called the "normal," to a surface (curve) is a vector perpendicular to its tangent plane (tangent line).
(a) Prove that the normal vector at $\left(x_{1}, f\left(x_{1}\right)\right)$ is $\left(f^{\prime}(x),-1\right)$.
(b) For a multivariable function $f(\vec{x})$, prove the normal vector at $\left(\vec{x}_{1}, f\left(\vec{x}_{1}\right)\right)$ is $\left(\nabla f(\vec{x})^{T},-1\right)$.
2. (70\%) Consider the function $f(x)=\sin (5 x)+x^{2}-3 x$ for $x \in[0,2]$
(a) Plot the function and print it.
(b) Write the Taylor expansion of $f(x)$ at $x=1$ to degree 3 and use Matlab to evaluate the difference of $f(1.5)$ and the Taylor expansion of $f(x)$ at $x=1.5$ for different degrees.
(c) Use Matlab to implement (1) the bisection method and (2) Newton's method to find the root of $f(x)$ to the precision $10^{-6}$ and compare their convergence. What initial guesses of Newton's method do you use? Will different initial guesses make different convergent results.

You may find some Matlab's sample codes in the last year's class website. http://www.cs.nthu.edu.tw/~cherung/teaching/2010cs5321/ homework/hw1.pdf

