

Test 1 for ISA5305

Spring 2017

1. Generate a 4 by 4 matrix A with each element an integer in $[0, 20]$, and a 4-dimensional integer column vector \mathbf{b} randomly from $[-10, 10]$, answer the following questions by using Matlab
 - (a) Solve \mathbf{x} for $A\mathbf{x}=\mathbf{b}$.
 - (b) Calculate the determinant of A .
 - (c) Find the rank of A .
 - (d) Find $\|A\|_p$, where $p=1, 2$, and ∞ .
 - (e) Find the characteristic polynomial of A .
 - (f) Find the eigenvalues of A .
 - (g) Find the singular values of A .
 - (h) Find the eigenvalues of A^tA .
 - (i) Find a QR-factorization for A (that is, $A=QR$).
 - (j) Solve \mathbf{y} for $R\mathbf{y}=Q^t\mathbf{b}$.
 - (k) Find $\|\mathbf{x}-\mathbf{y}\|_2$
2. Repeat Problem 1.(a~k) for a 3 by 3 matrix B .
3. For dataX.txt, find the best-fitting line.
4. For dataY.txt, find the best-fitting parabola (a quadratic curve).

Note: dataX.txt and dataY.txt could be downloaded from my lecture website.