

(1.)

```
// Boolean definition
#define TRUE 1
#define FALSE 0

// Recursive version
int check_recursive(A, left, right)
{
    if(left >= right)
        return TRUE;

    if(A[left] != A[right])
        return FALSE;
    else
        return check_recursive(A, left+1, right-1);
}
```

```
// Iterative version
int check_iterative(A, left, right)
{
    while(left < right)
    {
        if(A[left] != A[right])
            return FALSE;
        left++;
        right--;
    }
    return TRUE;
}
```

(2.)

```
void printback(A, n)
{
    // notice that in a C-like program, the last element is A[n - 1], not A[n]
    if(n > 0)
    {
        printf("%c", A[n - 1]);
        printback(A, n - 1);
    }
}
```

```

    }
    return;
}

```

Actually, we do not care your “Index-Error” if you have made some.

(3.)

```

void merge(X, Y, X, m, n)
{
    int index_x = 0;    // index of X
    int index_y = 0;    // index of Y
    int index_z = 0;    // index of Z

    // the core of “merge”
    // this part usually left some numbers which need to be attached to the end of Z
    while(index_x < m && index_y < n)
    {
        if(X[index_x] <= Y[index_y])
        {
            Z[index_z] = X[index_x];
            index_x++;
        }
        else
        {
            Z[index_z] = Y[index_y];
            index_y++;
        }
        index_z++;
    }

    // after the merge step, X or Y still should have some numbers
    // attach these numbers to the end of Z
    if(index_x < m)    // rest part of X
        while(index_x < m)
        {
            Z[index_z] = X[index_x];
            index_x++;
            index_z++;
        }
}

```

```

else    //rest part of Y
    while(index_y < n)
    {
        Z[index_z] = Y[index_y];
        index_y++;
        index_z++;
    }

    return;
}

```

(4.)

```
#define MAX_STACK_SIZE 1000
```

```
char stack[MAX_STACK_SIZE]; // the character stack
```

```
int top; // the top pointer of the stack
```

```
// the “clear stack” operation
```

```
void clear_stack(void)
```

```
{
    top = 0;
    return;
}
```

```
// the “push” operation
```

```
void push(char ch)
```

```
{
    stack[top] = ch;
    top++;
    return;
}
```

```
// the “pop” operation
```

```
char pop(void)
```

```
{
    if(top <= 0)
        ERROR(“Stack Empty!”);
    else

```

```

    {
        top--;
        return stack[top];
    }
}

```

// it's OK if you didn't define the Stack operation as above

// the TextEditor core

// notice that this function process a line at a time

// it returns the parsed line as a string. (that is, a character string)

```
char *TextEditor(void)
```

```

{
    char ch;

    scanf("%c", &ch); // read first character
    while(ch != '\n') // terminate if the end of the line is reached
    {
        if(ch == '&')
            clear_stack();
        else if(ch == '#')
            pop();
        else
            push(ch);

        scanf("%c", &ch); // read next character
    }
    stack[top] = '\0';
    return stack; // stack should contain the processed text
}

```

(5.)

a.

outer loop => $O(\log(n))$

inner loop => $O(m)$

overall => $O(m * \log(n))$

b.

$O(\log(n))$

(6.)

Here, let the right-most element in “stack” be the “Top”.

a.

push(1), stack = { 1 }, output = “”

push(2), stack = { 1, 2 }, output = “”

pop(), stack = { 1 }, output = “2”

push(3), stack = { 1, 3 }, output = “2”

push(4), stack = { 1, 3, 4 }, output = “2”

pop(), stack = { 1, 3 }, output = “24”

push(5), stack = { 1, 3, 5 }, output = “24”

push(6), stack = { 1, 3, 5, 6 }, output = “24”

pop(), stack = { 1, 3, 5 }, output = “246”

pop(), stack = { 1, 3 }, output = “2465”

pop(), stack = { 1 }, output = “24653”

pop(), stack = { }, output = “246531”

Done, possible.

b.

push(1), stack = { 1 }, output = “”

pop(), stack = { }, output = “1”

push(2), stack = { 2 }, output = “2”

push(3), stack = { 2, 3 }, output = “2”

pop(), stack = { 2 }, output = “13”

push(4), stack = { 2, 4 }, output = “13”

push(5), stack = { 2, 4, 5 }, output = “13”

push(6), stack = { 2, 4, 5, 6 }, output = “13”

pop(), stack = { 2, 4, 5 }, output = “136”

Now, we expect the next popped element to be “4”, but the top element is 5.

Thus, it’s impossible.

(7.)

a.

the most expected answer should be $((\text{rear} + n - \text{front}) \bmod n)$

if you write “ $(\text{rear} > \text{front}) ? (\text{rear} - \text{front}) : n + \text{rear} - \text{front}$ ” or a short if-else construct, it’s acceptable.

b.

$$n + n^2 \Rightarrow O(n^2)$$

$$\log(n) + n \Rightarrow O(n)$$

$$\log(n!) \text{ is bounded by } \log(n^n) = n \cdot \log(n) \Rightarrow O(n \cdot \log(n))$$

$$2^n \Rightarrow O(2^n)$$

$$\text{since } O(2^n) > O(n^2) > O(n \cdot \log(n)) > O(n),$$

$$2^n > n + n^2 > \log(n!) > \log(n) + n$$

c.

$$A[1, 2] \text{ at } 4143 \Rightarrow A[1, 0] \text{ at } 4141$$

$$A[2, 6] \text{ at } 4154 \Rightarrow A[2, 0] \text{ at } 4148$$

$$A[1, 0] \sim A[2, 0] \Rightarrow 4148 - 4141 = 7 \text{ element}$$

thus, we know $c = 7$, which is critical for computing the address of $A[6, 3]$

we can first compute the address of $A[0, 0]$ and then compute the address of $A[6, 3]$

$$A[0, 0] \text{ should at } (4141 - 7) = 4134$$

$$A[6, 3] \text{ at } (4134 + 6 \cdot 7 + 3) = 4179$$

d.

$$a * b + c + d * e - f * g$$

- | | | |
|----|-------|---------------|
| 1. | ----- | ab* |
| 2. | ----- | ab*c+ |
| 3. | ----- | ab*c+de* |
| 4. | ----- | ab*c+de*+ |
| 5. | ----- | ab*c+de*+fg* |
| 6. | ----- | ab*c+de*+fg*- |

(8.)

Here, let the right-most element in “stack” be the “Top”.

$$bcde^*+a^*, a = 2, b = 2, c = 5, d = 3, e = 7$$

$$\text{push}(b), \text{stack} = \{b\}$$

$$\text{push}(c), \text{stack} = \{b, c\}$$

$$\text{push}(d), \text{stack} = \{b, c, d\}$$

$$\text{push}(e), \text{stack} = \{b, c, d, e\}$$

$$\text{operation } * \text{ and } \{b, c, \underline{d}, \underline{e}\} \Rightarrow \text{pop } d \text{ and } e, d * e = 3 * 7 = 21, \text{push}(21),$$

$$\text{stack} = \{b, c, 21\}$$

$$\text{operation } + \text{ and } \{b, \underline{c}, \underline{21}\} \Rightarrow \text{pop } c \text{ and } 21, c + 21 = 5 + 21 = 26, \text{push}(26),$$

$$\text{stack} = \{b, 26\}$$

$$\text{push } a, \text{stack} = \{b, 26, a\}$$

operation - and {b, 26, a} => pop 26 and a, $26 - a = 26 - 2 = 24$, push(24)

=> stack = {b, 24}

operation * and {b, 24} => pop b and 24, $b * 24 = 2 * 24 = 48$, push(48)

=> stack = {48}

The result is 48.