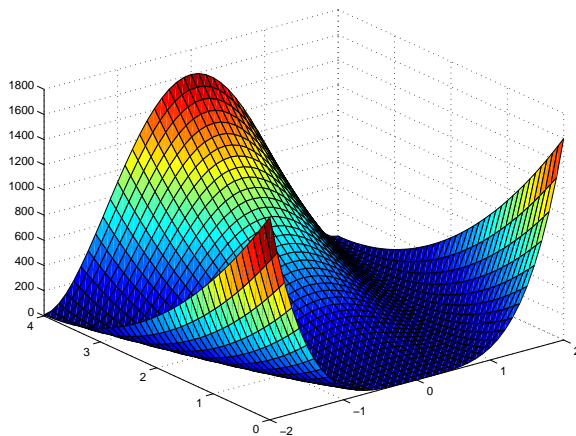


CS5321 Numerical Optimization Homework 3

Due April 11

1. (100%) The Rosenbrock function $f(x, y) = (1 - x)^2 + 100(y - x^2)^2$ is shown below, whose minimizer is at $(1, 1)$.¹



- (a) Derive the gradient and the Hessian of $f(x, y)$. (hand in this by next Thursday.)
- (b) Implement the backtracking line-search method, and make it a function. Your input should at least include
- The current solution \vec{x}_k .
 - The search direction \vec{p}_k .
 - The function that can evaluate $f(\vec{z})$ for a given \vec{z} .
 - The function that can evaluate $\nabla f(\vec{z})$ for a given \vec{z} .

and your output is the step length α that satisfies the Wolfe conditions or the Goldstein condition. (Just choose one to implement.)

- (c) Implement (1) the steepest descent method (2) Newton's method (3) SR1 or BFGS (4) CG or truncated Newton (CG with limited iterations). Use your line search algorithm to find the best step length. Use $(x_0, y_0) = (-1.2, 1.0)$ as the initial guess and compare their results. (Do not use any symbolic computation of Matlab, like `sub` or `diff`, or `eval`. Write your own function, gradient, and Hessian subroutines, and use them in your code. Also, do NOT implement your own linear solvers or rank 1 updates. Use $H \setminus \vec{b}$ or $B \setminus \vec{p}$ in Newton's method and SR1.)

¹You can find reference of this function in MO and Wikipedia.